


# (abstract) Algebra 1

*A bout of Nostalgia?* See [past Abstract Algebra courses](#).

## Welcome

. Our [Teaching Page](#) has important information for my students. (It has the [Notes](#), [Exams and Links](#) from all of my previous courses.)

The *Teaching Page* has my **schedule**, LOR guidelines, and [Usually Useful Pamphlets](#). One of them is the [Checklist](#)  (pdf) which gives pointers on competent mathematical writing. Further information is at our class-archive URL (I email this private URL directly to students).

Quantifiers  $\forall$  and  $\exists$  ("for all" and "there exists") are like nitroglycerin, in that one little mis-step leads to the whole thing blowing up in your face.

*There is no partial credit when it comes to Explosives and Quantifiers.*

-JLF King

In all of my courses, **attendance is absolutely required** (excepting illness and religious holidays). In the unfortunate event that you miss a class, *you are responsible* to get all **Notes / Announcements / TheWholeNineYards** from a classmate, or several. All my classes have a **substantial class-participation grade**.

- **First week of class:** Memorize the [Math-Greek alphabet \(pdf\)](#). which we will use in class frequently.
- **First week of class:** Read and thoroughly understand [Set-builder notation](#) (up through "Equivalent predicates...").
- **First week of class:** Work through this [Practice-prereq \(pdf\)](#) to see what you need to review.
- A useful reference is [Group Notes \(pdf\)](#). ~~UPDATED~~ [Thursday, 21Nov2019]  
 See also [Burnside's lemma \(W\)](#) and its application to [Counting necklaces \(W\)](#).  
 We will discuss [commutator of two elements \(W\)](#) in a group.
- In one convenient location: All **0** [Alg quizzes so far \(pdf\)](#), ~~[[?]]~~ ~~UPDATED~~  
*In this "quizzes" link, please have read the binomial/multinomial conventions on page 2, together with Operations on Sets.*
- In order to facilitate for students posting solns to our Archive, in addition to Gallian, we will use [Abstract Algebra: Theory and Applications by Thomas Judson \(2016 Edition\)](#), an online text made publicly available by its author. Students will be posting solns both from their edition of Gallian, as well as Judson text, as well as any interesting algebra problems students create.
- [Does Zero = One? \(pdf\)](#). Here are some ~~proofs~~ *poofs* about which you can post to our Archive.

- *Nostalgia?*: See [past Abstract Algebra incarnations](#).

This will help you decide if my teaching-style is the right style for you.

As the semester progresses, you will also need to print-out a few pages of handouts that I have prepared for you.

We will cover some material that is not in our text; in particular, applications of group-theory for solving certain games and puzzles.

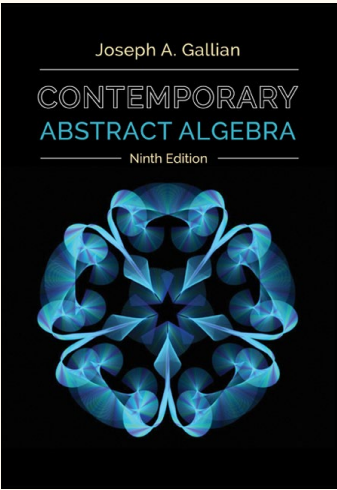
Our textbook is *Contemporary Abstract Algebra 9<sup>th</sup> edition*.

*AUTHOR:* Joseph A. Gallian

*ISBN:* 9781305657960

*YEAR:* 2017

*PUBLISHER:* Houghton Mifflin



It is [available from the publisher](#) as well as from online booksellers.

The various Math czars who help out.

COMPUTER&PROJECTOR

TIME

MEMORY/TELEPATHY

BLACKBOARD

E-PROBS

??



ALGEBRA ON “THE WEB”

See also [general math references](#).

- [Alg. T/F at Gallian's website](#).
- [Group Explorer](#). I have not reviewed this.

Lyrics for [The Klein Four – Finite Simple Group](#) are:

The path of love is never smooth  
But mine's continuous for you  
You're the upper bound in the chains of my heart  
You're my Axiom of Choice, you know it's true  
  
But lately our relation's not so well-defined  
And I just can't function without you

I'll prove my proposition and I'm sure you'll find  
We're a finite simple group of order two

I'm losing my identity  
I'm getting tensor every day  
And without loss of generality  
I will assume that you feel the same way

Since every time I see you, you just quotient out  
The faithful image that I map into  
But when we're one-to-one you'll see what I'm about  
'Cause we're a finite simple group of order two

Our equivalence was stable,  
A principal love bundle sitting deep inside  
But then you drove a wedge between our two-forms  
Now everything is so complexified

When we first met, we simply connected  
My heart was open but too dense  
Our system was already directed  
To have a finite limit, in some sense

I'm living in the kernel of a rank-one map  
From my domain, its image looks so blue,  
'Cause all I see are zeroes, it's a cruel trap  
But we're a finite simple group of order two


I'm not the smoothest operator in my class,  
But we're a mirror pair, me and you,  
So let's apply forgetful functors to the past  
And be a finite simple group, a finite simple group,  
Let's be a finite simple group of order two  
(Oughter: "Why not three?")

I've proved my proposition now, as you can see,  
So let's both be associative and free  
And by corollary, this shows you and I to be  
Purely inseparable. Q. E. D.

Lyrics by *Matt Salomone*


## End-of-semester Algebra (Individual Optional Project) [IOP-D \(pdf\)](#)



...will be due, slid<sup>u</sup>nder  my office door (Little Hall 402, Northeast corner) , no later than

**2PM, Thursday, ??Dec2022**

**T**he IOP must be *carefully typed*, but diagrams may be hand-drawn.

**F**or the typesetting, one possibility is the (free) [mathematics-typesetting language](#) .

**At all times** have a **paper copy** you can hand-in; I do **NOT** accept electronic versions. Print out a copy *each day*, so that you *always* have the latest version to hand-in; this, in case your printer or computer fails. (You are **too old** for "My dog ate my homework.")

Please follow the guidelines on the [Checklist](#)  (pdf, 3pages) to earn full credit.

[JK Home page](#)



