

## MTG6257/MAT4930 SYLLABUS – SPRING, 2024

**Lecture Times and Location:** MWF period 7th (1:55 pm - 2:45 pm), Little Hall, Room 225

**Instructor:** Luca F. Di Cerbo  
<https://people.clas.ufl.edu/ldicerbo/>

**Instructor's Office:** Little Hall 476

**Office Hours:** Monday 4th Period (10:40 - 11:30 am), Wednesday 4th Period (10:40 - 11:30 am), and by appointment.

**Instructor's Email:** ldicerbo@ufl.edu

**COURSE TITLE:** Differential Geometry 2.

**PREREQUISITES:** Differential Geometry 1.

### COURSE OBJECTIVES

We will continue the study of modern Differential and Riemannian Geometry. You will be able to communicate such concepts in writing and through short oral presentations. This course will expose you to modern graduate level mathematics which also plays an important role in theoretical physics, such as **General Relativity** and **String Theory**.

### MAIN TEXTBOOKS

- Manfredo P. do Carmo, Riemannian Geometry. Mathematics: Theory & Applications. *Birkhäuser Boston, Inc., Boston, MA*, 1992.
- Isaac Chavel, Eigenvalues in Riemannian Geometry. Pure and Applied Mathematics, 115. *Academic Press, Inc., Orlando, FL*, 1984.

### Other References

- Shing-Tung Yau. Some function-theoretic properties of complete Riemannian manifold and their applications to geometry. *Indiana Univ. Math. J.* 25 (1976), no. 7, 659–670.
- Peter Petersen, Riemannian Geometry. Third edition. Graduate Texts in Mathematics, 171. *Springer, Cham*, 2016.

## COURSE DESCRIPTION

Below is a list of topics we will be covering.

Riemann Curvature tensor and Bianchi Identities. Main Notions of Curvature: Sectional Curvature, Ricci Curvature, and Scalar Curvature. Jacobi fields, Conjugate Points, and Klingenberg Lemma. Second Fundamental Form of a Riemannian Submanifold, Hopf-Rinow Theorem, and the Theorem of Hadamard. The theorems of Bonnet-Myers and Synge-Weinstein. Green's Formulas and Laplacian on Manifolds. Harmonic functions on complete manifolds (following S.-T. Yau). Fundamental group of manifolds of negative curvature.

We will cover the material from **Chapters 3, 4, 5, 6, 7, 9, 12** of the Main Textbook (Riemannian Geometry, by do Carmo). Tentatively we will also cover some aspects of the research papers by S.-T. Yau listed above under "Other References".

## COURSE SCHEDULE

We will follow the progression of topics listed in the "Course Description" section. Roughly, this is the weekly schedule

- Week 1: Finish Chapter 3;
- Weeks 2 – 5: Chapters 4–5;
- Weeks 6 – 7: Chapter 6;
- Weeks 8 – 9: Chapter 7;
- Week 10 – Spring Break;
- Weeks 11 – 13: Chapter 9;
- Weeks 14 – 16: Chapter 12 and Review.

The course schedule is subject to adjustments depending on my interaction with the audience. For a more detailed breakdown of the material to be covered, I refer you to the **e-learning Canvas** page for this class.

## ATTENDANCE POLICY, CLASS EXPECTATIONS, and MAKE-UP POLICY

I consider attendance to be a crucial part of the instructions for this class, and you should actively participate to our in person sessions. Students shall be excused from class following the UF guidelines. Also, due to the unprecedented circumstances we still face this semester, I will try to be flexible following a case-by-case approach when it comes to attendance, late and make-up work. Excused absences must be consistent with university policies in the Graduate Catalog and require appropriate documentation.

Additional information can be found here:

<https://catalog.ufl.edu/ugrad/current/regulations/info/attendance.aspx>

## EVALUATION OF GRADES

- Homework, presentations, and attendance (60%).
- One mid-term exam (15%). The date and format are to be determined.
- Final exam (25%). The date and format are to be determined.

## GRADING POLICY

- **Grading:** The grading scale is from 0 to 100 points. The final grade is based on homework and attendance, midterms, and a final. A student may also request the possibility of giving a final oral presentation at the end of the semester for extra credit. Grading in this class is consistent with UF policies available at: <https://catalog.ufl.edu/UGRD/academic-regulations/grades-grading-policies/>
- **Policy on Late and Make-up Work:** Students shall be excused from class or other scheduled academic activity to observe a religious holy day of their faith with prior notification to the instructor. Students shall be permitted a reasonable amount of time to make up the material or activities covered in their absence. Students shall not be penalized due to absence from class or other scheduled academic activity because of religious observances. Students who are absent from classes or examinations because of illness should contact their instructors. The Student Health Care Center (SHCC) <https://shcc.ufl.edu/> can provide a medical excuse note only if their providers are involved in the medical care of a student who must be absent from class for three or more days for medical reasons. A student who has a medical reason that results in fewer than three days of absence from class should talk with his/her professor rather than ask for an excuse note from the SHCC. If a professor subsequently requires a note for a medical absence of fewer than three days, then the professor must provide the SHCC with a written request on UF departmental letterhead.
- **Grade Return Timing:** Each homework, midterm, and final will be graded within 3 to 5 business days. Moreover, within the same time frame I will communicate the corresponding grade via a **Canvas** email (preferred option for security reasons).

- **Point Range for this Class:** A: 90% – 100%, A-: 85% – 89%, B+: 80% – 84%, B: 75% – 79%, B-: 70% – 74%, C+: 66% – 69%, C: 60% – 65%, C-: 56% – 59%, D+: 52% – 55%, D: 48% – 51%, D-: 45% – 47%, F: 0% – 44%.

## IN-CLASS RECORDING

- Students are allowed to record video or audio of class lectures. However, the purposes for which these recordings may be used are strictly controlled. The only allowable purposes are (1) for personal educational use, (2) in connection with a complaint to the university, or (3) as evidence in, or in preparation for, a criminal or civil proceeding. All other purposes are prohibited. Specifically, students may not publish recorded lectures without the written consent of the instructor.
- A “class lecture” is an educational presentation intended to inform or teach enrolled students about a particular subject, including any instructor-led discussions that form part of the presentation, and delivered by any instructor hired or appointed by the University, or by a guest instructor, as part of a University of Florida course. A class lecture does not include lab sessions, student presentations, clinical presentations such as patient history, academic exercises involving solely student participation, assessments (quizzes, tests, exams), field trips, private conversations between students in the class or between a student and the faculty or lecturer during a class session.
- Publication without permission of the instructor is prohibited. To “publish” means to share, transmit, circulate, distribute, or provide access to a recording, regardless of format or medium, to another person (or persons), including but not limited to another student within the same class section. Additionally, a recording, or transcript of a recording, is considered published if it is posted on or uploaded to, in whole or in part, any media platform, including but not limited to social media, book, magazine, newspaper, leaflet, or third party note/tutoring services. A student who publishes a recording without written consent may be subject to a civil cause of action instituted by a person injured by the publication and/or discipline under UF Regulation 4.040 Student Honor Code and Student Conduct Code.

## STUDENTS REQUIRING ACCOMMODATIONS

Students with disabilities requesting accommodations should first register with the Disability Resource Center (352-392-8565, <https://www.dso>).

ufl.edu/drc) by providing appropriate documentation. Once registered, students will receive an accommodation letter which must be presented to the instructor when requesting accommodation. Students with disabilities should follow this procedure as early as possible in the semester.

## **COURSE EVALUATIONS**

Students are expected to provide professional and respectful feedback on the quality of instruction in this course by completing course evaluations online via GatorEvals at <https://gatorevals.aa.ufl.edu/>. Guidance on how to give feedback in a professional and respectful manner is available at <https://gatorevals.aa.ufl.edu/students/>. Students will be notified when the evaluation period opens, and can complete evaluations through the email they receive from GatorEvals, in their Canvas course menu under GatorEvals, or via <https://ufl.bluera.com/ufl/>. Summaries of course evaluation results are available to students at <https://gatorevals.aa.ufl.edu/public-results/>.

## **UNIVERSITY HONESTY POLICY**

UF students are bound by The Honor Pledge which states, “We, the members of the University of Florida community, pledge to hold ourselves and our peers to the highest standards of honor and integrity by abiding by the Honor Code. On all work submitted for credit by students at the University of Florida, the following pledge is either required or implied: “On my honor, I have neither given nor received unauthorized aid in doing this assignment.” The Honor Code:

(<https://www.dso.ufl.edu/sccr/process/student-conduct-honor-code/>)

specifies a number of behaviors that are in violation of this code and the possible sanctions. Furthermore, you are obligated to report any condition that facilitates academic misconduct to appropriate personnel. If you have any questions or concerns, please consult with the instructor or TAs in this class.

## **COVID-19 STATEMENT**

In response to COVID-19, the following recommendations are in place to maintain your learning environment, to enhance the safety of our in-classroom interactions, and to further the health and safety of ourselves, our neighbors, and our loved ones.

- If you are not vaccinated, get vaccinated. Vaccines are readily available and have been demonstrated to be safe and effective against the

COVID-19 virus. Visit [one.ufl.edu](http://one.ufl.edu) for screening / testing and vaccination opportunities.

- If you are sick, stay home. Please call your primary care provider if you are ill and need immediate care or the UF Student Health Care Center at 352-392-1161 to be evaluated.
- Course materials will be provided to you with an excused absence, and you will be given a reasonable amount of time to make up work.

## DIVERSITY STATEMENT

The Mathematics Department is committed to diversity and inclusion of all students. We acknowledge, respect, and value the diverse nature, background and perspective of students and believe that it furthers academic achievements. It is our intent to present materials and activities that are respectful of diversity: race, color, creed, gender, gender identity, sexual orientation, age, religious status, national origin, ethnicity, disability, socioeconomic status, and any other distinguishing qualities.

## STUDENT PRIVACY

There are federal laws protecting your privacy with regards to grades earned in courses and on individual assignments. For more information, please see:

<http://registrar.ufl.edu/catalog0910/policies/regulationferpa.html>

## CAMPUS RESOURCES

### *Health and Wellness*

#### **U Matter, We Care:**

If you or a friend is in distress, please contact [umatter@ufl.edu](mailto:umatter@ufl.edu) or 352 392-1575 so that a team member can reach out to the student.

**Counseling and Wellness Center:** <http://www.counseling.ufl.edu/cwc>, and 392-1575; and the University Police Department: 392-1111 or 9-1-1 for emergencies.

**Sexual Assault Recovery Services (SARS)**, Student Health Care Center, 392-1161.

**University Police Department** at 392-1111 (or 9-1-1 for emergencies), or <http://www.police.ufl.edu/>.

### *Academic Resources*

**E-learning technical support**, 352-392-4357 (select option 2) or e-mail to Learning-support@ufl.edu. <https://lss.at.ufl.edu/help.shtml>.

**Career Resource Center**, Reitz Union, 392-1601. Career assistance and counseling. <https://www.crc.ufl.edu/>.

**Library Support**, <http://cms.uflib.ufl.edu/ask>. Various ways to receive assistance with respect to using the libraries or finding resources.

**Teaching Center**, Broward Hall, 392-2010 or 392-6420. General study skills and tutoring. <https://teachingcenter.ufl.edu/>.

**Writing Studio**, 302 Tigert Hall, 846-1138. Help brainstorming, formatting, and writing papers. <https://writing.ufl.edu/writing-studio/>.

**Student Complaints Campus**: [https://www.dso.ufl.edu/documents/UF\\_Complaints\\_policy.pdf](https://www.dso.ufl.edu/documents/UF_Complaints_policy.pdf).

**On-Line Students Complaints**:

<http://www.distance.ufl.edu/student-complaint-process>.