# Work Krishnaswami Alladi Department of Mathematics Search Krishnaswami Alladi Home MAT 6932 Seminar in Number Theory Fall 2015

# Irrationality, Diophantine Approximations and Transcendence

MWF 4th period (10:40-11:30am) - LIT 201 - FALL 2015

# INSTRUCTOR:

Curriculum Vitae

> The Ramanujan Journal

Related Links

MAP 2302 Fall 2015
 Publications

Courses

Research

Activities

Krishnaswami Alladi 304 Little Hall (352) 294-2290 email: alladik@ufl.edu

The SASTRA Ramanujan Prize

MAT 6932 Seminar in Number Theory Fall 2015

# OFFICE HOURS:

M and W 6th period (12:50 - 1:40 pm) in LIT 304 and by appointment.

#### PREREQUISITES:

## COURSE DESCRIPTION:

The study of irrational numbers dates back to Greek antiquity. Yet the subject remains an active area of research today. Although "almost all" real numbers are irrational, it is very difficult to establish the irrationality of a given number. We will study a variety of techniques which will help in confirming the irrationality of different classes of numbers starting with Dirichte's fundamental criterion for irrationality. Following this, we will discuss irrationality criteria utilizing series and product representations of reals due to Engel, Cantor, and Sylvester, regular and general continued fraction expansions, and Farey fractions. We will present various proofs of the irrationality of important numbers such as e and  $\pi$ , and the Bessel functions like the tingonometric, hyperbolic, and the Bessel functions like the tingonometric, hyperbolic, and the Bessel functions like the tingonometric, hyperbolic, divide the concept of irrationality of ansures. This is the subject of Diophantine approximations. It will be shown that the truncations of the regular continued fraction expansion of real numbers generate the sequence of "best approximations", but it is very difficult to determine the continued fraction expansion of real numbers and product the approximations of a given irrational. We will develop methods to obtain effective irrationality measures alto social with expension of a given irrational with a sequence of this approach is the irrationality of the Riemann zeta function at the odd integer 3 – a fact conjectured long ago but established only in 1978. The study of irrationality many solutions whereas the Thue equation  $x^3 - 2y^2 = 1$  has only a finitely many integer solutions. Thus the subject of Diophantine approximations is closely associated with the theory of Diophantine equations. As part of our study of Diophantine approximations, we will lanch the study of transcendental numbers by showing first that e is transcendental, and more generaly that the result of Lindemann that the exponential functi

# TEXT:

No assigned text. I will use my own notes. A number of texts will be given as references.

#### GRADING:

Grades will be based on a few homework assignments, and seminars that students will have an opportunity to give.

#### ACCOMODATION FOR STUDENTS WITH DISABILITIES:

Students requesting classroom accommodation must first register with the Dean of Students Office. The Dean of Students Office will provide documentation to the student who must then provide this documentation to the Instructor when requesting accommodation. WebMail eLearning | ISIS | MyUFL | Campus Map | News | Calendar | Directory | WebSiteListing | Aek UF Disability Services | Privacy Policy | Recudations | Make a Gift @ 2015 University of Florids, Generalite, EL33611 ( Re20 382-3861 | Page Updated August 21, 2015 This page uses Google Analytics (Google Privacy Policy)

UF

